## Syllabus for Introduction to Fractional Calculus Non-credit 20 hours of Lectures and Exercises by Prof Francesco MAINARDI The Division of Applied Mathematics, Brown University April 14 -May 14, 2015

The 2-hour lectures will be held by Professor F. Mainardi on Tuesdays and Thursdays from 9:00 AM to 11:00 AM in Room 110 at 182 George Street

The course is scheduled for 5 weeks starting on Tuesday April 14 and ending on Thursday May 14, 2015.

The class/home works will be graded by a teaching assistant.

This mini-course is for Graduate students, however, advanced juniors and seniors are welcomed. No registration required.

Hours	Lecture contents	
1-2	Laplace and Fourier transforms	Exercises
3-4	Eulerian and Mittag-Leffler functions	Exercises
5-6	Error, Bessel and Wright functions	Exercises
7-8	Fractional calculus in $R^+$	Exercises
9-10	Fractional calculus in $R$	Exercises
11 - 12	Abel integral equations	Exercises
13-14	Fractional relaxation and oscillations	Exercises
15 - 16	Time fractional diffusion wave equations	Exercises
17-18	Space fractional diffusion-wave equations	Exercises
19-20	Time-space fractional diffusion-wave equations	Exercises

Suggested texts

- 1. G. B. Arfken, H. J. Weber and F. E. Harris, *Mathematical Methods for Physicists*, (7-th ed.), Elsevier, Oxford, 2012.
- D. Baleanu, K. Diethelm, E. Scalas and J. Trujillo, Fractional Calculus: Models and Numerical Methods World Scientific, Singapore, 2012.
- B. Davies, Integral Transforms and Their Applications, (3-rd ed.), Springer-Verlag, New York, 2002.
- R. Gorenflo, A. A Kilbas, F. Mainardi and S. V. Rogosin, *Mittag-Leffler Functions. Related Topics and Applications*, Springer, Berlin, 2014.
- R. Gorenflo and F. Mainardi, Fractional calculus, integral and differential equations of fractional order, in A. Carpinteri and F. Mainardi (Editors), Fractals and Fractional Calculus in Continuum Mechanics, Springer Verlag, Wien, 1997, pp. 223-276. [E-print http://arxiv.org/abs/0805.3823]

- A.A Kilbas, H.M. Srivastava, and J.J. Trujillo, J.J. (2006). Theory and Applications of Fractional Differential Equations, Elsevier, Amsterdam, 2006
- F. Mainardi, Fractional calculus, some basic problems in continuum and statistical mechanics, in A. Carpinteri and F. Mainardi (Editors), Fractals and Fractional Calculus in Continuum Mechanics, Springer Verlag, Wien,1997, pp. 291-348. [[E-print http://arxiv.org/abs/1201.0863]
- 8. F. Mainardi, *Methods and Problems in Mathematical Physics*. Lectures Notes, University of Bologna.
- F. Mainardi, Fractional Calculus and Waves in Linear Viscoelasticity, Imperial College Press, London, 2010.
- I. Podlubny, Fractional Differential Equations, Academic Press, San Diego, 1999.